## International Journal of Advanced Research in Computer Science RESEARCH PAPER

## Available Online at www.ijarcs.info

# Quality Controlled ECG Signal Compression using Genetic Algorithm 

Vibha Aggarwal<br>Department of Electronics \& Communication Engineering, COEM, Punjabi University Neighborhood Campus, Rampura Phul, Punjab, India<br>vibha_ec@yahoo.co.in

Manjeet Singh Patterh<br>Department of Electronics \& Communication Engineering, UCOE, Punjabi University, Patiala, Punjab, India<br>pattarms@ieee.org


#### Abstract

In this paper, calculations of threshold using genetic algorithm (GA) is studied. From the results, it can be found that the threshold value calculated using GA is such that the actual PRD (Percent root mean square difference) after threshold is almost equal to the UPRD (User specified PRD). First ECG signal is transformed using wavelet transform (WT) and discrete cosine transform (DCT). The transformed coefficients (TC) are then thresholded by genetic algorithm. The thresholding is done in a way so that error between actual PRD and UPRD remains within the specified limits.


Keywords: ECG Signal, quality controlled compression, Discrete Cosine Transform, Wavelet Transform, Genetic Algorithm.

## I. INTRODUCTION

Many quality controlled ECG compression algorithms have recently been developed that gives good performance [1]-[8]. Among the reported algorithms [1]-[8], the threshold value is calculated by the bisection algorithms (BA) in order to match the UPRD within the tolerance. Most of them are using the WT. In 2003, Benzid et al. [5] presented quality controlled ECG compression based on wavelet transform, after decomposition the resultant coefficients are subjected to an iterative threshold until a fixed percentage target of wavelet coefficients to be zeroed is reached. Then, the Look-up table is made to store the zero and non-zero coefficients (NZC). NZC are quantized by linear quantizer. The NZC and look up table encoding is done by Huffman coding. Blanco-Velasco et al., [3] developed a filter bankbased algorithm for quality controlled ECG compression. The procedure is same as [5] but here the bisection algorithm (BA) is used for calculation. And this method for threshold calculation found to be better than [5]. In 2006, Benzid et al. [1] used wavelet transform and Max-Lloyd quantizer. Chen et al. [8] presents quality controlled ECG compression based on wavelet transform, these coefficients are quantized with a uniform scalar dead zone quantizer and Exp-Golomb and Golomb-Rice coding is used to code the lengths of runs of the zero coefficients and nonzero coefficients respectively. Benzid et al. [2] proposed the effective method of ECG compression based on the adaptive wavelet coefficients quantization combined with a modified two-role encoder.

The algorithm is same as explained in [1] but the NZC are encoded by two role encoder and here quantizer is linear. Blanco-Velasco et al. [4] methodology is same as [5] this paper used the Wavelet Packet transform instead of wavelet transform. Benzid et al., [6] represents ECG compression using block-based DCT. To identify the optimal threshold value the combination of False Position (Regula Falsi) and bisection technique is used. Here the linear quantizer is used and encoding is done by arithmetic coding. In this paper the threshold value is calculated by the GA. GAs are computational models inspired from biological evolution,
which is based on the mechanics of natural genetics and natural selection. The back- bone of every GA is the reproduction of an original population, the performance of crossover and mutation and the selection of the best [9]. For the performance analysis, the metrics like compression ratio (CR) and PRD are used. CR is defined as the ratio of the number of bits used to represent the original signal to the number of bits used to represent the compressed signal [4] and PRD is calculated as [5]:
$P R D=100 \times \sqrt{\frac{\sum_{i=1}^{N}\left(x_{i}-\hat{x}_{i}\right)^{2}}{\sum_{i=1}^{N} x_{i}^{2}}}$
(1.1) Where $x_{i}$ and $\hat{X}_{i}$ are
the $\mathrm{i}^{\text {th }}$ sample of original and reconstructed ECG signal of length $N$ [5].

## II. METHODOLOGY

The proposed technique is implemented in three steps: (i) the TC are thresholded using genetic algorithm and (ii) the thresholded coefficients are quantized and (iii) Final stage is the entropy coder that provides the final compressed bitstream. The pseudo code for the algorithm is explained as follows [1][2].

Step 0: Initialization; Get the UPRD; Select the threshold in the range [THmin, THmax] where the range may be initialized by [*TCmin, **TCmax]. Where *TCmin is minimum value of TC and **TCmax is maximum value of TC. Get the convergence precision $\epsilon=0.01$. Calculate the mean. Subtract the mean from the original signal. Transform the zero mean ECG signal using DCT and WT .

Step 1: Take a copy of TC. $\mathrm{x}=$ [ THmin THmax] Fitness function $=100 \times\left(x(1)^{2}-x(2)\right)^{2}+(1-x(1))^{2}$ And select threshold using GA

Step 2: Inverse TC. Add the mean to the inverse coefficients.

Step 3: Compute the PRD
Step 4: if $a b s(P R D-U P R D) \geq \epsilon$. Then go to Step 1
Step5: Construct the binary lookup table to represent the zero and non-zero coefficients obtained after
thresholding in Step1. This binary lookup table is encoded using Huffman coding.

Step6: The non-zero coefficients are quantized using Max-Lloyd algorithm followed by Arithmetic coding.

Step7: End.

## III. RESULTS

The efficiency of the proposed algorithm is tested by well known ECG database, MIT-BIH Arrhythmia. Each record contains 11 bit resolution and 360 Hz a sampling frequency. In the WT, ECG signal is decomposed to four levels using biorthogonal swapped filters. The results presented in Table 1, 2, 3 and 4 represents the CR at fixed $\operatorname{PRD}=0.5, \mathrm{PRD}=1, \mathrm{PRD}=2$ and $\mathrm{PRD}=3$ respectively for different ECG signals using BA and GA. From the numerical results, it can be observed that PRD before quantization (BPRD) is nearly equal to fixed PRD (UPRD) and PRD after quantization (QPRD) using BA and GA. Table 5 and Figure 1 compares the proposed method to that compression methods reported in the literature which is best threshold-based ECG compression. For comparison the average CR and the average PRD of the proposed method are taken according to that reported in the literature. Testing dataset is of 2 min duration long ( 43200 samples) lead extracted from records $100,101,102,103,107,109,111$, 115, 117, 118 and 119. This dataset has been chosen for Table 5 and Figure 1 because it has been used in the literature. Figure 1, Table 5 and Table 6 conclude that the proposed method gives better CR as compared to that reported in [2]-[8].

But as far as BA is concerned the CR of the proposed method using GA is almost same. For example, in case of record MIT-BIH 121 at $\mathrm{UPRD}=0.5, \mathrm{QPRD}=0.52, \mathrm{CR}$ is 17.85 for DCT from Table 1 and at UPRD= $0.5, \mathrm{QPRD}=$ 0.50 , CR is 15.67 for WT from Table 2 with BA and with GA at $U P R D=0.5, \mathrm{QPRD}=0.50, \mathrm{CR}$ is 18.21 for DCT from Table 3 and at $\mathrm{UPRD}=0.5, \mathrm{QPRD}=0.50$, CR is 15.67 for WT from Table 4. It can be observed from the result that in case of GA the actual PRD is very close to the UPRD. So, in general GA is recommended over BA. But during the implementation of GA based threshold calculations it has been observed that GA based method requires more time for calculations of threshold at high UPRD. Therefore, it is recommended that GA method for threshold calculation should be used in case of low UPRD.

## IV. CONCLUSION

In this paper, to calculate the threshold value with the help of genetic algorithm has been studied. The method of calculating threshold value is very good and it gives final

PRD which is within the specified error as compared to UPRD. But computational time is more in case of GA as compared to that of BA for higher values of UPRD. So, GA is recommended for low PRD ECG compression. So, GA is recommended for low PRD ECG compression.
The method gives high performance for ECG compression due to the combined effect of transforms (DCT and WT), thresholding algorithm, non-uniform quantizer, look-up table encoded by Huffman coding and non-zero quantized coefficients are encoded by Arithmetic coding. But computational time is more in case of GA as compared to that of BA for higher values of UPRD.

## V. REFERENCES

[1]. R. Benzid, F. Marir and N. E. Bouguechal, "Qualitycontrolled compression method using wavelet transform for electrocardiogram signals", Int. J. of Biomed. Sciences, 2006, 1, (1),pp. 28-33.
[2]. R. Benzid, F. Marir and N. E. Bouguechal, "Electrocardiogram compression method based on the adaptive wavelet coefficients quantization combined to a modified two-role encoder", IEEE Signal Process. Lett., 2007, 1-4.
[3]. M. Blanco-Velasco, F. Cruz-Roldan, J. I. Godino-Llorente and K. E. Barner, "ECG compression with retrived qualtiy guranteed", Electron. Lett., 2004, 40, (23).
[4]. M. Blanco-Velasco, F. Cruz-Roldan, J. I. Godino-Llorente and K. E. Barner, "Wavelet packets feasibility study for the design of an ECG compressor", IEEE Trans. on Biomed. Eng., 2007, 54, (4), pp. 766-769.
[5]. R. Benzid, F. Marir, M. Benyoucef and D. Arar, "Fixed percentage of wavelet coefficients to be zeroed for ECG compression", Electron. Lett., 2003, 39,(11), pp. 830-831.
[6]. R. Benzid, A. Messaoudi, A. Boussaad, "Constrained ECG compression algorithm using block-based discrete cosine transfrom", Digital Signal Processing, 2008, 18, pp. 56-64.
[7]. Z. Lu, D. Y. Kim and W. A. Pearlman, "Wavelet compression of ECG signals by the set partitioning in hierarchical trees algorithm", IEEE Trans. on Biomed. Eng., 2000,47, (7), pp. 849-856.
[8]. J. Chen, J. Ma, Y. Zhang and X. Shi, "ECG compression based on wavelet transform and Golomb coding", Electronics Letters, 2006, 42 (6).
[9]. N. E. Mastorakis, I. F. Gonos and M. N. S. Swamy, "Design of two-dimensional recursive filters using genetic algorithms", IEEE Trans. on Circuits and Syst.-I: Fund. Theory and App., 2003, 50, (5), pp. 634-639.

Table 1: Performance of ECG compression with BA using DCT on different ECG signals

| DCT, ${ }^{1}$ Qbits=14, Samples=43200, Time=2 min, |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Signal | ${ }^{2}$ UPRD=0.5 |  |  | ${ }^{2}$ UPRD $=1$ |  |  | ${ }^{2}$ UPRD $=2$ |  |  | ${ }^{2}$ UPRD $=3$ |  |  |
|  | ${ }^{3}$ BPRD | ${ }^{4}$ QPRD | ${ }^{5} \mathrm{CR}$ | ${ }^{3}$ BPRD | ${ }^{4}$ QPRD | ${ }^{5} \mathrm{CR}$ | ${ }^{3}$ BPRD | ${ }^{4}$ QPRD | ${ }^{5} \mathrm{CR}$ | ${ }^{3}$ BPRD | ${ }^{4}$ QPRD | ${ }^{5} \mathrm{CR}$ |
| 121 | 0.49 | 0.52 | 17.85 | 1.00 | 1.00 | 37.66 | 1.99 | 1.99 | 50.55 | 2.99 | 2.99 | 51.69 |
| 122 | 0.49 | 0.53 | 15.16 | 0.99 | 0.99 | 22.27 | 2.01 | 2.01 | 24.63 | 3.00 | 3.00 | 26.89 |
| 205 | 0.50 | 0.54 | 12.60 | 1.00 | 1.01 | 26.47 | 1.98 | 1.98 | 29.72 | 2.99 | 3.00 | 30.18 |
| 103 | 0.50 | 0.52 | 10.41 | 0.99 | 1.00 | 13.83 | 1.99 | 1.99 | 19.14 | 2.98 | 2.98 | 20.86 |
| 104 | 0.49 | 0.55 | 13.37 | 0.99 | 1.02 | 15.47 | 1.98 | 1.98 | 17.83 | 2.97 | 2.97 | 17.74 |
| 221 | 0.49 | 0.52 | 10.33 | 0.99 | 1.00 | 11.79 | 1.99 | 1.98 | 20.57 | 3.02 | 3.02 | 23.94 |
| 201 | 0.50 | 0.53 | 11.05 | 0.99 | 1.01 | 12.82 | 1.98 | 1.98 | 23.77 | 2.98 | 2.98 | 28.86 |
| 203 | 0.49 | 0.51 | 11.64 | 1.00 | 1.01 | 14.89 | 2.01 | 2.01 | 15.75 | 2.97 | 2.97 | 16.43 |
| 233 | 0.50 | 0.51 | 11.49 | 1.00 | 1.00 | 18.36 | 1.99 | 1.99 | 20.06 | 2.97 | 2.97 | 20.61 |
| 109 | 0.49 | 0.52 | 11.21 | 0.99 | 1.00 | 17.53 | 1.99 | 1.99 | 23.84 | 3.00 | 3.00 | 27.99 |
| ${ }^{1}$ Qbits- bits used for quantization${ }^{2}$ UPRD- user defined PRD |  |  |  |  |  |  |  |  |  |  |  |  |

Table 2: Performance of ECG compression with BA using WT on different ECG signals

| WT, ${ }^{1}$ Qbits=14, Samples=43200, Time=2 min, |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Signal | ${ }^{2}$ UPRD=0.5 |  |  | ${ }^{2}$ UPRD $=1$ |  |  | ${ }^{2}$ UPRD $=2$ |  |  | ${ }^{2}$ UPRD=3 |  |  |
|  | ${ }^{3}$ BPRD | ${ }^{4}$ QPRD | ${ }^{5} \mathrm{CR}$ | ${ }^{3}$ BPRD | ${ }^{4}$ QPRD | ${ }^{5} \mathrm{CR}$ | ${ }^{3}$ BPRD | ${ }^{4}$ QPRD | ${ }^{5} \mathrm{CR}$ | ${ }^{3}$ BPRD | ${ }^{4}$ QPRD | ${ }^{5} \mathrm{CR}$ |
| 121 | 0.50 | 0.50 | 15.67 | 1.00 | 1.00 | 28.58 | 1.99 | 1.99 | 49.66 | 2.97 | 2.97 | 54.29 |
| 122 | 0.50 | 0.50 | 11.92 | 0.99 | 0.99 | 16.33 | 1.98 | 1.98 | 28.94 | 3.01 | 3.01 | 33.25 |
| 205 | 0.49 | 0.49 | 10.98 | 1.00 | 1.00 | 16.81 | 1.99 | 2.00 | 24.60 | 3.01 | 3.01 | 30.49 |
| 103 | 0.49 | 0.49 | 9.92 | 0.99 | 0.99 | 11.58 | 1.98 | 1.98 | 18.62 | 3.00 | 3.00 | 27.77 |
| 104 | 0.50 | 0.50 | 10.38 | 0.99 | 0.99 | 11.19 | 1.99 | 1.99 | 15.18 | 3.00 | 3.00 | 20.19 |
| 221 | 0.50 | 0.50 | 10.33 | 0.99 | 0.99 | 10.68 | 1.99 | 1.99 | 14.28 | 2.98 | 2.99 | 18.27 |
| 201 | 0.50 | 0.50 | 10.83 | 0.99 | 0.99 | 11.15 | 1.99 | 1.99 | 15.86 | 2.98 | 2.98 | 23.18 |
| 203 | 0.49 | 0.50 | 10.27 | 0.99 | 1.00 | 11.20 | 2.00 | 2.00 | 14.27 | 2.99 | 2.99 | 18.33 |
| 233 | 0.50 | 0.50 | 10.61 | 0.99 | 1.00 | 15.41 | 1.99 | 1.99 | 18.08 | 2.97 | 2.97 | 19.65 |
| 109 | 0.49 | 0.49 | 10.34 | 1.00 | 1.00 | 13.61 | 2.00 | 2.00 | 23.42 | 3.00 | 3.00 | 28.61 |
| ${ }^{1}$ Qbits- bits used for quantization ${ }^{2}$ UPRD- user defined PRD <br> ${ }^{3}$ BPRD- PRD before quantization <br> ${ }^{4}$ QPRD- PRD after quantization <br> ${ }^{5} \mathrm{CR}$-Compression ratio |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |

Table 3: Performance of ECG compression with GA using DCT on different ECG signals

| DCT, ${ }^{1}$ Qbits=14, Samples=43200, Time=2 min |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Signal |  | UPRD=0 |  |  | ${ }^{2}$ UPRD $=1$ |  |  | ${ }^{2}$ UPRD $=$ |  |  | ${ }^{2}$ UPRD $=$ |  |
|  | ${ }^{3}$ BPRD | ${ }^{4}$ QPRD | ${ }^{5} \mathrm{CR}$ | ${ }^{3}$ BPRD | ${ }^{4}$ QPRD | ${ }^{5} \mathrm{CR}$ | ${ }^{3}$ BPRD | ${ }^{4}$ QPRD | ${ }^{5} \mathrm{CR}$ | ${ }^{3}$ BPRD | ${ }^{4}$ QPRD | ${ }^{5} \mathrm{CR}$ |
| 121 | 0.5084 | 0.5067 | 18.2153 | 0.9985 | 0.9997 | 37.4200 | 1.9935 | 1.9945 | 50.5532 | 2.9982 | 2.9983 | 51.6971 |
| 122 | 0.4912 | 0.4911 | 15.1030 | 0.9944 | 0.9941 | 22.2806 | 2.0097 | 2.0097 | 24.6371 | 3.0017 | 3.0017 | 26.8900 |
| 205 | 0.5098 | 0.5100 | 12.7222 | 0.9971 | 0.9958 | 26.3531 | 1.9981 | 1.9982 | 29.6259 | 3.0030 | 3.0021 | 30.2444 |
| 103 | 0.5000 | 0.4989 | 10.4200 | 0.9906 | 0.9899 | 13.7436 | 2.0022 | 2.0045 | 19.1737 | 2.9980 | 2.9967 | 20.9302 |
| 104 | 0.5061 | 0.5177 | 13.3572 | 0.9989 | 1.0008 | 15.4688 | 1.9909 | 1.9959 | 17.8325 | 2.9974 | 2.9928 | 17.7525 |
| 221 | 0.4948 | 0.4975 | 10.3466 | 1.0003 | 0.9980 | 11.8091 | 2.0097 | 2.0083 | 20.6681 | 3.0057 | 3.0051 | 24.0194 |
| 201 | 0.5100 | 0.5057 | 11.0573 | 1.0057 | 1.0012 | 12.8349 | 1.9962 | 1.9948 | 23.9613 | 2.9982 | 2.9956 | 28.9756 |
| 203 | 0.5086 | 0.5112 | 11.6975 | 1.0065 | 1.0078 | 14.9134 | 2.0035 | 2.0025 | 15.7434 | 2.9964 | 2.9985 | 16.4863 |
| 233 | 0.5020 | 0.5068 | 11.5027 | 0.9935 | 0.9943 | 18.3107 | 1.9969 | 1.9983 | 20.0743 | 2.9928 | 2.9956 | 20.6322 |
| 109 | 0.4914 | 0.4973 | 11.1696 | 1.0001 | 1.0004 | 17.5325 | 2.0028 | 1.9999 | 23.8842 | 3.0016 | 3.0018 | 28.0321 |
| 112 | 0.4961 | 0.4977 | 19.7671 | 1.0005 | 0.9994 | 34.1576 | 1.9974 | 1.9982 | 38.8489 | 3.0100 | 3.0111 | 40.5788 |
| 217 | 0.5042 | 0.5158 | 12.3160 | 0.9960 | 1.0015 | 17.5948 | 2.0082 | 2.0110 | 18.2882 | 3.0019 | 3.0023 | 19.0568 |
|  Qbits- bits used for quantization ${ }^{2}$ UPRD- user defined PRD <br> ${ }^{3}$ BPRD- PRD before quantization ${ }_{4}$ QPRD- PRD after quantization ${ }^{5}$ CR-Compression ratio |  |  |  |  |  |  |  |  |  |  |  |  |

Table 4: Performance of ECG compression with GA using WT on different ECG signals

|  |  |  |  |  | ${ }^{1}$ Qbits= | amples | 200, Tim | min |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Signal |  | ${ }^{\text {UPRD }}=0$ |  |  | UPRD= |  |  | ${ }^{2}$ UPRD $=$ |  |  | ${ }^{2}$ UPRD |  |
|  | ${ }^{3}$ BPRD | ${ }^{4}$ QPRD | ${ }^{5} \mathrm{CR}$ | ${ }^{3}$ BPRD | ${ }^{4}$ QPRD | ${ }^{5} \mathrm{CR}$ | ${ }^{3}$ BPRD | ${ }^{4}$ QPRD | ${ }^{5} \mathrm{CR}$ | ${ }^{3}$ BPRD | ${ }^{4}$ QPRD | ${ }^{5} \mathrm{CR}$ |
| 121 | 0.5041 | 0.5031 | 15.6770 | 1.0049 | 1.0049 | 28.5577 | 1.9937 | 1.9937 | 49.5413 | 2.9939 | 2.9940 | 54.4954 |
| 122 | 0.4937 | 0.4928 | 11.8350 | 1.0099 | 1.0093 | 16.4315 | 1.9984 | 1.9980 | 29.1319 | 2.9927 | 2.9928 | 32.9817 |
| 205 | 0.4976 | 0.4993 | 10.9817 | 0.9937 | 0.9938 | 16.6901 | 1.9914 | 1.9917 | 24.6065 | 2.9973 | 2.9973 | 30.0000 |
| 103 | 0.4905 | 0.4985 | 9.9298 | 0.9947 | 0.9946 | 11.5880 | 2.0031 | 2.0040 | 18.8153 | 3.0013 | 3.0015 | 27.7700 |
| 104 | 0.5011 | 0.5075 | 10.3810 | 1.0086 | 1.0074 | 11.2160 | 1.9978 | 1.9947 | 15.1840 | 2.9958 | 2.9977 | 20.1698 |
| 221 | 0.4957 | 0.4985 | 10.3376 | 0.9902 | 0.9856 | 10.6624 | 1.9977 | 1.9945 | 14.2857 | 3.0033 | 3.0025 | 18.3164 |
| 201 | 0.5018 | 0.5097 | 10.8039 | 0.9908 | 0.9963 | 11.1528 | 2.0009 | 2.0033 | 15.9121 | 3.0020 | 3.0032 | 23.4320 |
| 203 | 0.5021 | 0.5074 | 10.2786 | 0.9961 | 0.9953 | 11.1907 | 2.0055 | 2.0082 | 14.2754 | 3.0092 | 3.0095 | 18.4186 |
| 233 | 0.4949 | 0.4951 | 10.5713 | 0.9933 | 0.9942 | 15.3647 | 1.9902 | 1.9909 | 18.0712 | 2.9905 | 2.9897 | 19.7342 |
| 109 | 0.4945 | 0.5263 | 10.4467 | 1.0014 | 1.0042 | 13.6145 | 1.9964 | 1.9969 | 23.3766 | 3.0011 | 3.0000 | 28.5989 |
| 112 | 0.5091 | 0.5101 | 16.4270 | 1.0044 | 1.0052 | 25.2122 | 1.9933 | 1.9933 | 38.0525 | 2.9986 | 2.9969 | 43.5484 |
| 217 | 0.4991 | 0.4957 | 10.0236 | 0.9946 | 0.9944 | 12.8488 | 2.0046 | 2.0046 | 19.4882 | 3.0089 | 3.0090 | 25.7589 |
| ${ }^{1}$ Qbits- bits used for quantization${ }^{3}$ BPRD- PRD before quantization $\quad{ }^{2}$ UPRD- user defined PRD${ }^{4}$ QPRD- PRD after quantization |  |  |  |  |  |  |  |  |  |  |  |  |

Table 5: Compression results

| Proposed method with DCT | PRD | 2.6427 | 2.8776 | 3.4578 | 3.7278 | 4.1512 | 4.8009 | 5.7648 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | CR | 24.0514 | 24.2419 | 24.6988 | 24.9055 | 25.2669 | 25.7487 | 26.4071 |
| Proposed method with WT | PRD | 2.6405 | 2.8808 | 3.4575 | 3.7304 | 4.1420 | 4.7945 | 5.7614 |
|  | CR | 27.1251 | 28.1654 | 30.2581 | 31.0241 | 32.2080 | 33.3796 | 34.6589 |
| Benzid [6] | PRD | 2.66 | 2.89 | 3.48 | 3.77 | 4.18 | 4.81 | 5.79 |
|  | CR | 10.84 | 11.46 | 13.45 | 14.29 | 15.43 | 17.10 | 19.64 |
| Benzid [2] | PRD | -- | 2.89 | 3.51 | -- | -- | 4.84 | -- |
|  | CR | -- | 10.70 | 12.61 | -- | -- | 15.95 | -- |
| Blanco-Velasco [4] | PRD | 2.69 | 2.90 | 3.45 | 3.73 | 4.16 | 4.80 | 5.77 |
|  | CR | 9.62 | 10.65 | 12.38 | 12.98 | 13.76 | 14.78 | 16.05 |
| Chen [8] | PRD | 2.72 | 2.91 | 3.47 | 3.73 | 4.15 | 4.79 | 5.75 |
|  | CR | 11.59 | 12.48 | 14.45 | 15.51 | 17.12 | 19.53 | 22.87 |
| Blanco-Velasco [3] | PRD | 2.72 | 2.91 | 3.47 | 3.73 | 4.15 | 4.79 | 5.75 |
|  | CR | 9.41 | 10.33 | 11.84 | 12.44 | 13.19 | 14.13 | 15.32 |
| Benzid [5] | PRD | 2.64 | 2.88 | 3.46 | 3.73 | 4.15 | 4.80 | 5.76 |
|  | CR | 7.05 | 8.28 | 10.89 | 11.62 | 12.46 | 13.49 | 14.74 |
| Lu [7] | PRD | 1.19 | 1.56 | 2.46 | 2.96 | 3.57 | 4.85 | 6.49 |
|  | CR | 4:1 | 5:1 | 8:1 | 10:1 | 12:1 | 16:1 | 20:1 |

Table 6: Comparison with other methods

| Method | Signal | CR | PRD |
| :---: | :---: | :---: | :---: |
| Proposed Method with DCT | 117 | 33.1658 | 1.1805 |
|  |  | 33.8269 | 2.5446 |
|  |  | 33.1658 | 0.9926 |
|  | 119 | 21.0714 | 5.1280 |
|  | 232 | 13.3154 | 0.3057 |
| Proposed Method with WT | 117 | 25.8036 | 1.1791 |
|  |  | 45.5871 | 2.5593 |
|  |  | 23.94 | 1.00 |
|  | 119 | 32.3353 | 5.1276 |
|  | 232 | 12.7852 | 0.3040 |
| Benzid [6] | 117 | 21.74 | 2.54 |
|  |  | 9.56 | 1.18 |
| Benzid [2] | 117 | 16.70 | 2.15 |
| Blanco-Velasco [4] | 232 | 7.35 | 5.00 |
| Chen [8] | 117 | 8.31 | 1.07 |
|  |  | 17.45 | 2.0 |
|  | 119 | 18.14 | 2.65 |
|  | 232 | 9.78 | 4.91 |
| Blanco-Velasco [3] | 117 | 8.24 | 1.1760 |
|  |  | 17.40 | 2.5359 |
|  | 119 | 18.02 | 5.0474 |
|  | 232 | 9.70 | 6.2806 |
| Benzid [1] | 117 | 27.93:1 | 1.04 |
| Benzid [5] | 117 | 16.24 | 2.55 |
|  | 119 | 17.43 | 5.1268 |
|  | 232 | 9.04 | 0.2981 |
| Lu[7] | 117 | 8 | 1.18 |



Figure. 1 Performance of proposed algorithm

